

For everyone's sake, please interrupt for clarification on any of these concepts during the talk (after they are introduced).

1. Printer. \*

```
type Printer a = a -> Doc
```

\* Doc is an abstract document representation.

2. Parser. †

```
newtype Parser a = Parser (String -> [(a, String)])
```

† The list here allows non-determinism (backtracking). The string in the result is the unparsed remainder.

3. Partial isomorphisms‡.

```
data Iso a b = Iso
  { apply    :: a -> Maybe b
  , unapply  :: b -> Maybe a
  }

```

‡ Isomorphism: A pair of functions  $f : A \rightarrow B$  and  $g : B \rightarrow A$  that are inverses such that:

1.  $f \circ g \equiv id_B$
2.  $g \circ f \equiv id_A$

4. IsoFunctor: the functor<sup>§</sup> from Iso to Hask (restricted to f).

```
class IsoFunctor f where
  (<$>) :: Iso a b -> f a -> f b
```

§ Functor: A principled way of taking a "thing" and "moving" it into a different context whilst preserving some notion of structure.

The canonical Haskell example is the Functor typeclass. Given two types  $(\forall a, b \in \text{Hask})$  that have a function between them  $(\exists f : a \rightarrow b)$  we can produce a functored function  $(\forall F \in \text{Functor}. F(f) : F(a) \rightarrow F(b))$ .

More formally: a functor,  $F$ , is a transformation between categories  $\mathcal{C}$  and  $\mathcal{D}$  that maps morphisms and objects in  $\mathcal{C}$  to morphisms and objects in  $\mathcal{D}$  such that a few rules hold given objects  $A, B \in \mathcal{C}$ :

1.  $F(f : A \rightarrow B) = F(f) : F(A) \rightarrow F(B)$
2.  $F(id_A) = id_{F(A)}$
3.  $F(f \circ g) = F(f) \circ F(g)$

5. ProductFunctor: a way to merge the output/input of two f's.

```
class ProductFunctor f where
  -- Left associative, applies before <$>
  infixr 6 <*>
  (<*>) :: f a -> f b -> f (a, b)
```

6. Alternative: try one failing that, the other.

```
class Alternative where
  (<|>) :: f a -> f a -> f a
```

7. Syntax: putting it all together.

```
class (IsoFunctor s, ProductFunctor s, Alternative s) => Syntax s where
  -- (<$>) :: Iso a b -> f a -> f b
  -- (<*>) :: f a -> f b -> f (a, b)
  -- (<|>) :: f a -> f a -> f a
  pure :: Eq a => a -> s a -- Eq for checking the value at runtime
```

```
class Syntax s => JsonSyntax s where
  -- Nest the first syntax within the second.
  runSub :: s v -> s Value -> s v
```

```
-- We need a concrete way to access the underlying Aeson Value types in
-- order to work with them.
value :: s Value
```